

# Dynamic and Adaptive Maintenance Policies for Complex Systems based on Real-Time Data

Gero Walter, Simme Douwe Flapper

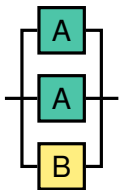
Eindhoven University of Technology, Eindhoven, NL

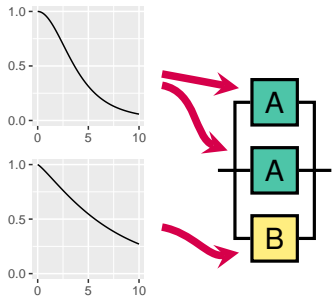
[g.m.walter@tue.nl](mailto:g.m.walter@tue.nl)

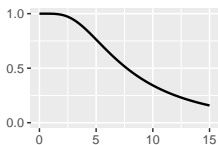
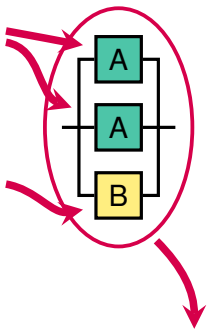
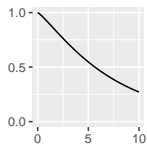
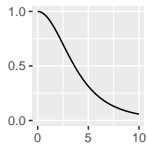


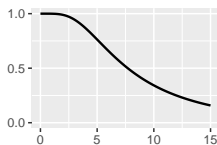
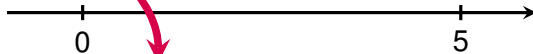
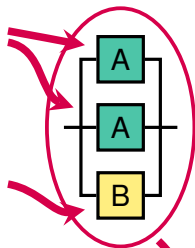
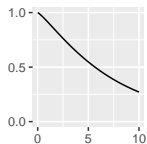
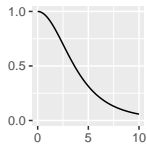
**DINALOG**  
Dutch Institute  
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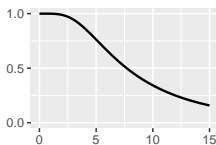
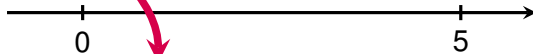
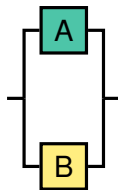
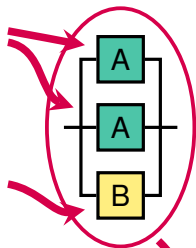
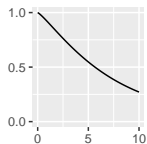
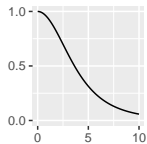
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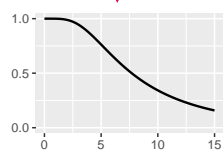
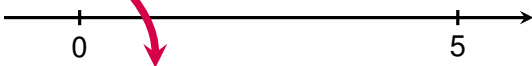
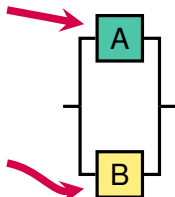
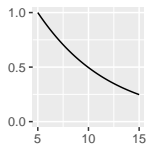
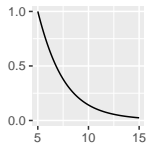
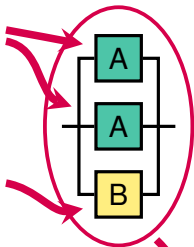
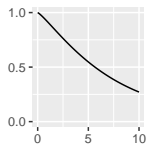
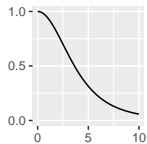




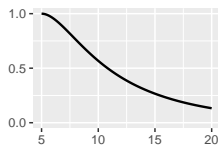
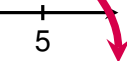
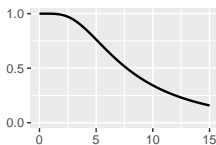
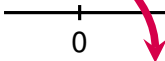
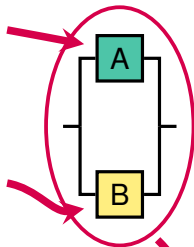
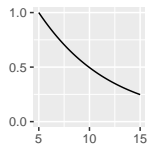
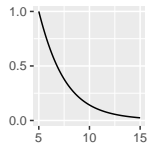
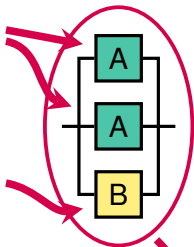
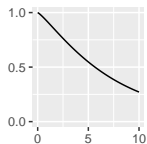
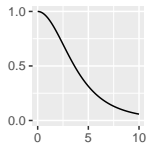




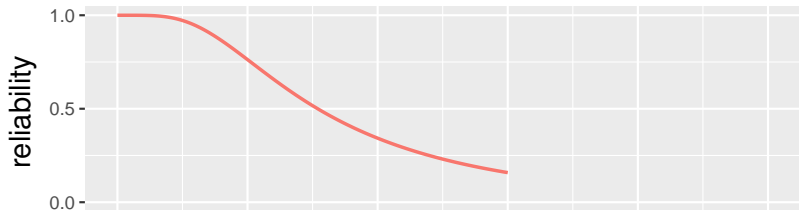


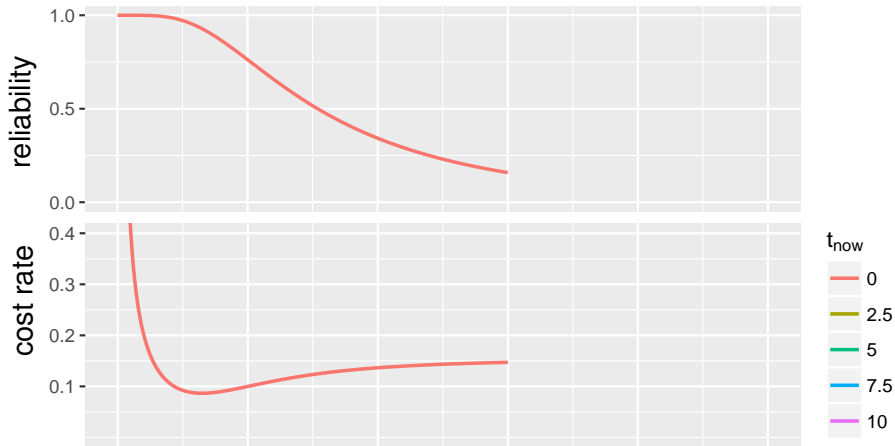


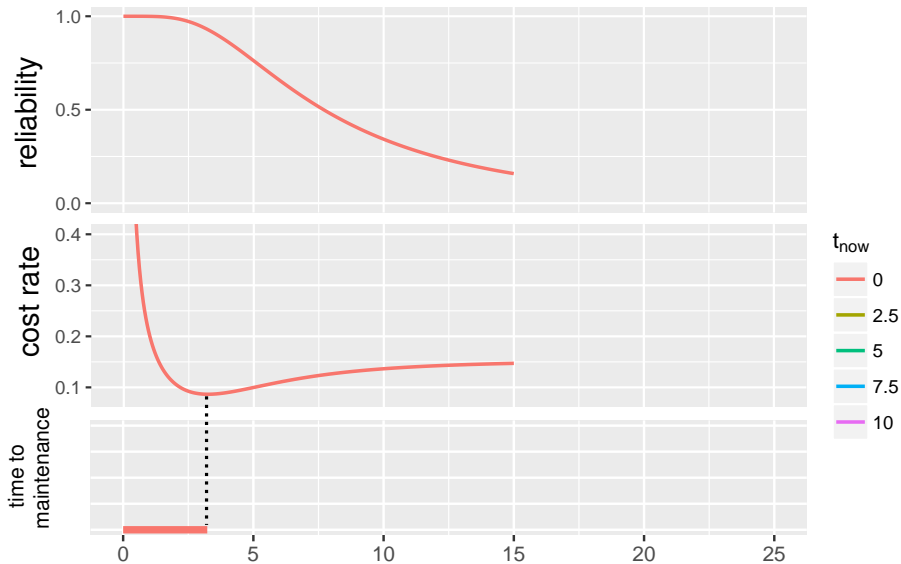
# Dynamic & Adaptive Residual Life Distributions

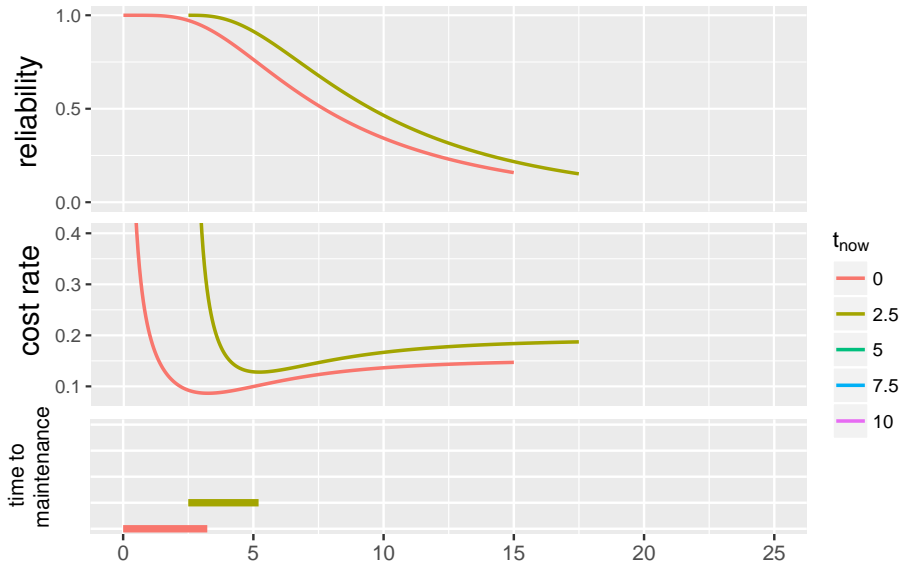


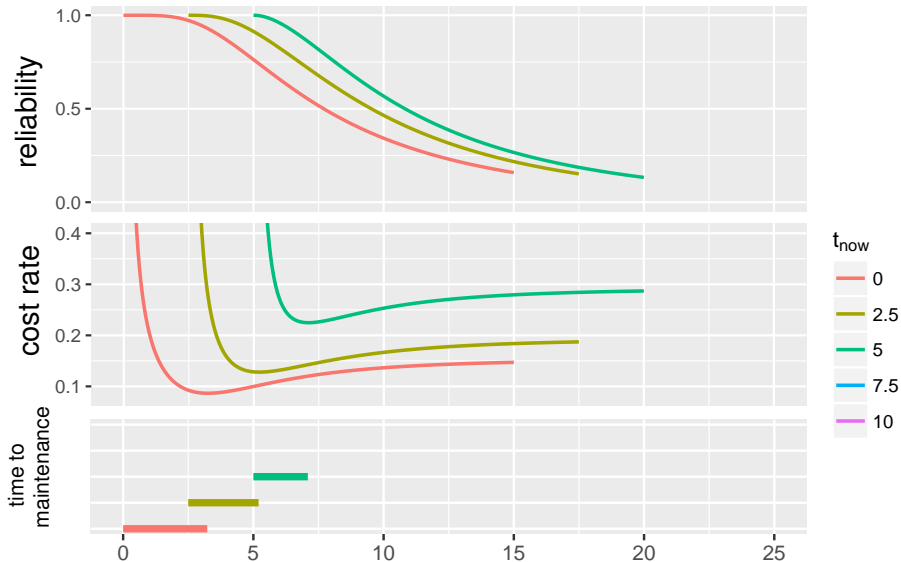


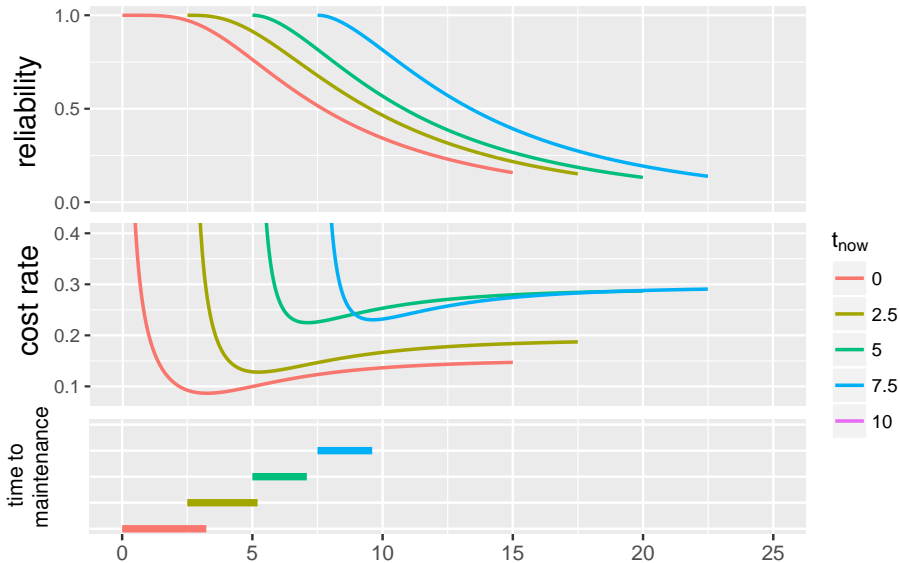


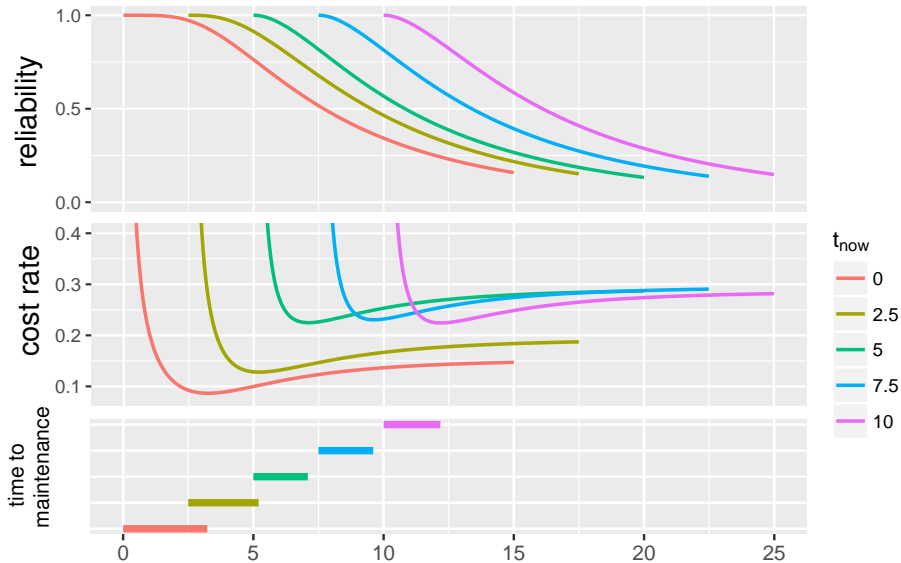






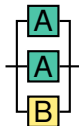






Inputs before start-up:

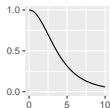
- ▶ system reliability block diagram





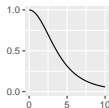
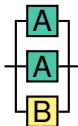
Inputs before start-up:

- ▶ system reliability block diagram
- ▶ for each component type:
  - Weibull shape parameter & MTTF from expert
  - expert confidence (how sure about MTTF)
  - optional: test data



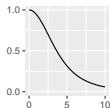
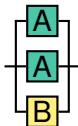
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  - optional: test data
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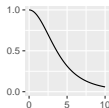
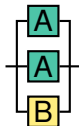


Input during run-time (preferred automatic):

- ▶ which components still work and which not

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Input during run-time (preferred automatic):

- ▶ which components still work and which not

Output:

- ▶ for any time during run-time:  
cost-optimal moment to repair the system (dynamic & adaptive)

$T_{\text{sys}}^{(t_{\text{now}})}$  (random) time of system failure given all info. at time  $t_{\text{now}}$

$R_{\text{sys}}^{(t_{\text{now}})}(t)$  corresponding reliability function

$c_k^{(t_{\text{now}})}$  number of type  $k$  components functioning at time  $t_{\text{now}}$

$K$  number of component types

$$R_{\text{sys}}^{(t_{\text{now}})}(t) = \sum_{l_1=0}^{c_1^{(t_{\text{now}})}} \cdots \sum_{l_K=0}^{c_K^{(t_{\text{now}})}} \underbrace{\Phi^{(t_{\text{now}})}(l_1, \dots, l_K)}_{\text{survival signature}} \prod_{k=1}^K \underbrace{P(C_t^k = l_k \mid n_k^{(0)}, y_k^{(0)}, t_k^{(t_{\text{now}})})}_{\text{Probability that } l_k \text{ of the } c_k^{(t_{\text{now}})} \text{ } \mathbf{k} \text{'s function}}$$

survival signature  
=  $P(\text{system functions} \mid \{l_k \mathbf{k}\}'\text{s function}\}^{1:K})$

Probability that  $l_k$  of the  
 $c_k^{(t_{\text{now}})}$   $\mathbf{k}$ 's function

$\tau$  decision variable (when to do maintenance?)

$T_{\text{sys}}^{(t_{\text{now}})}$  (random) time of system failure,  
with density  $f_{\text{sys}}^{(t_{\text{now}})}(t)$  and reliability function  $R_{\text{sys}}^{(t_{\text{now}})}(t)$

$c_p$  cost of planned maintenance action

$c_u$  cost of unplanned maintenance action

$$g(\tau | T_{\text{sys}}^{(t_{\text{now}})} = t) = \begin{cases} c_p/\tau & \text{if } t \geq \tau & \text{(cost rate if failure after } \tau) \\ c_u/t & \text{if } t < \tau & \text{(cost rate if failure before } \tau) \end{cases}$$

$$g^{(t_{\text{now}})}(\tau) = \mathbb{E}[g(\tau | T_{\text{sys}}^{(t_{\text{now}})})] = \frac{c_p}{\tau} R_{\text{sys}}^{(t_{\text{now}})}(\tau) + c_u \int_0^{\tau} \frac{1}{t} f_{\text{sys}}^{(t_{\text{now}})}(t) dt$$

$$\tau_*^{(t_{\text{now}})} := \arg \min g^{(t_{\text{now}})}(\tau)$$